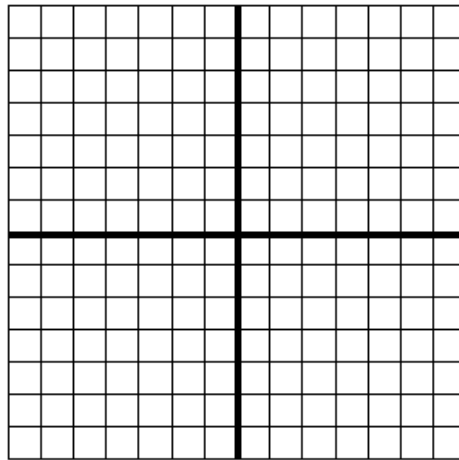


Basic or "parent" Graph: $y = 2^x$

Graph by a table of values:

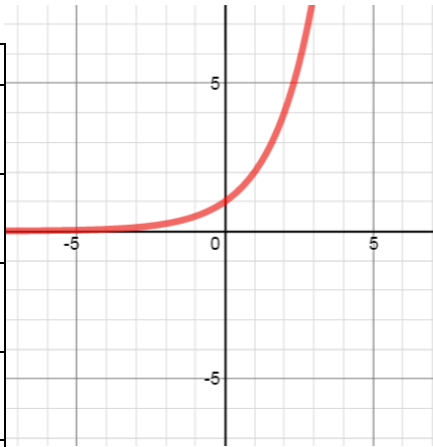
| x | $y = 2^x$ |
|-----|-----------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |



Important characteristics:

A. $y = 2^x + 3$

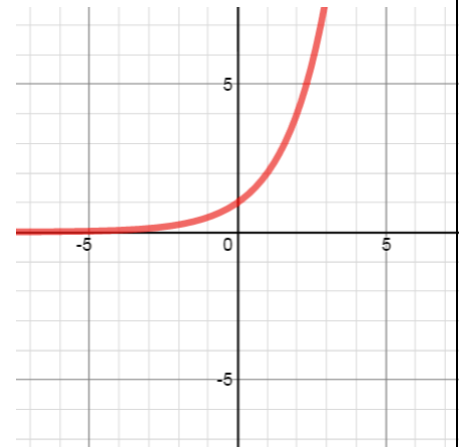
| x | $y = 2^x + 3$ |
|-----|---------------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |



Contrast to Parent Function:

B. $y = 2^x - 3$

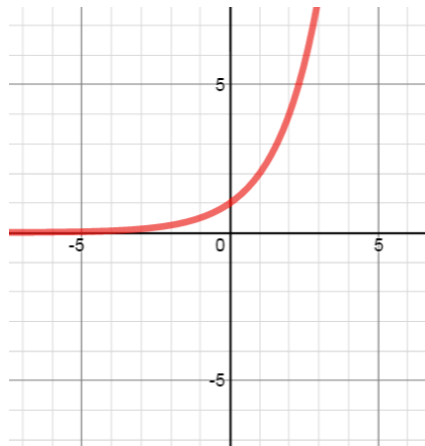
| x | $y = 2^x - 3$ |
|-----|---------------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |



Contrast to Parent Function:

C. $y = 2^{x+3}$

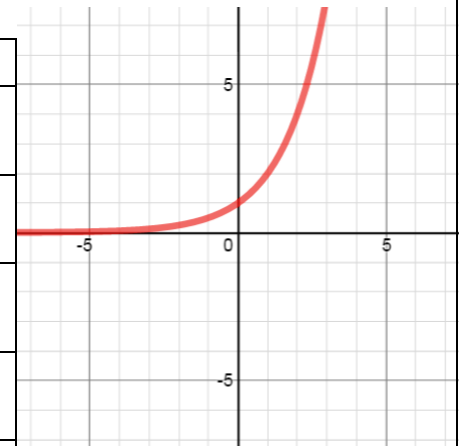
| x | $y = 2^{x+3}$ |
|-----|---------------|
| -5 | |
| -4 | |
| -3 | |
| -2 | |
| -1 | |



Contrast to Parent Function:

D. $y = 2^{x-3}$

| x | $y = 2^{x-3}$ |
|-----|---------------|
| 1 | |
| 2 | |
| 3 | |
| 4 | |
| 5 | |



Contrast to Parent Function:

E. $y = \left(\frac{1}{2}\right)^x$

| x | y = $\left(\frac{1}{2}\right)^x$ |
|----|----------------------------------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |

Contrast to Parent Function:

***CHALLENGE** $y = -2^x$

| x | y = -2^x |
|----|------------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |

Contrast to Parent Function:

GRAPHING EXPONENTIAL FUNCTIONS $f(x) = b^x$

When $b > 1$

When $0 < b < 1$

TRANSFORMING EXPONENTIAL FUNCTIONS

Exponential functions, as well as linear, quadratic, and polynomial functions, **can all undergo the same types of transformations.**

| Type of Transformation | Example <i>Parent function: $f(x) = 2^x$</i> | General Condition <i>Parent function: $f(x)$</i> |
|--|---|--|
| Vertical translation <i>(up or down)</i> | $g(x) = 2^x + 3$ (3 units up) $h(x) = 2^x - 1$ (1 unit down) | $f(x) + k$ $k > 0$ up $k < 0$ down |
| Horizontal translation <i>(to the left or right)</i> | $g(x) = 2^{(x-4)}$ (4 units right) $t(x) = 2^{(x+3)}$ (3 units left) | $f(x-h)$ $h > 0$ right $h < 0$ left [h is positive if it's right after the minus sign.] |
| Vertical stretch or compression | $g(x) = 3(2)^x$ (stretch) $h(x) = \frac{1}{3}(2)^x$ (compression) | $a f(x)$ $a > 1$ stretch compression $0 < a < 1$ |
| Reflection | $g(x) = -2^x$ | $-f(x)$ over x-axis ↑ opposite of |

Use the chart to answer the questions below.

1. How does the graph of $f(x) = 2.7^x$ compare to the graph of $g(x) = 2.7^x - 4$?

2. How does the graph of $f(x) = 2.7^x$ compare to the graph of $g(x) = 2.7^{(x-5)}$?
