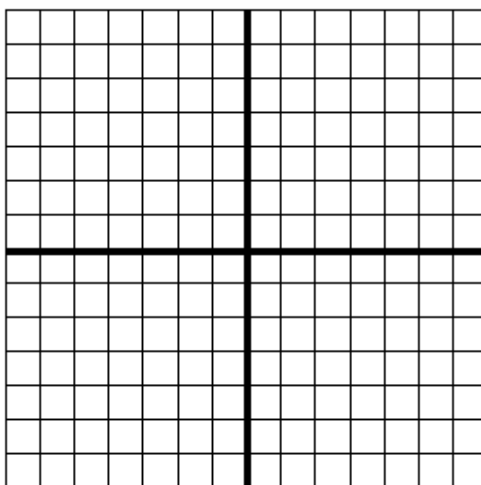


Graphing Quadratic Functions in Vertex Form/Transformations

Basic or "parent" Graph: $f(x) = x^2$

Graph by a table of values:

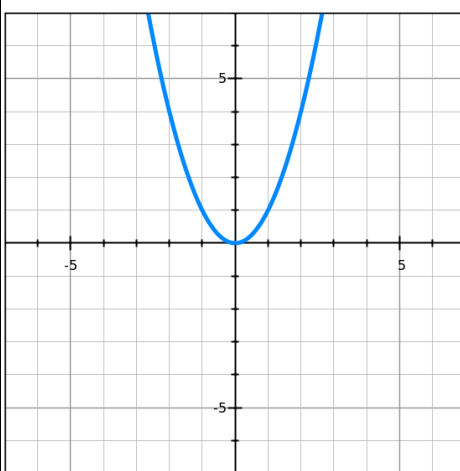
x	$f(x) = x^2$
-2	
-1	
0	
1	
2	



Important characteristics:

A. $g(x) = x^2 + 3$

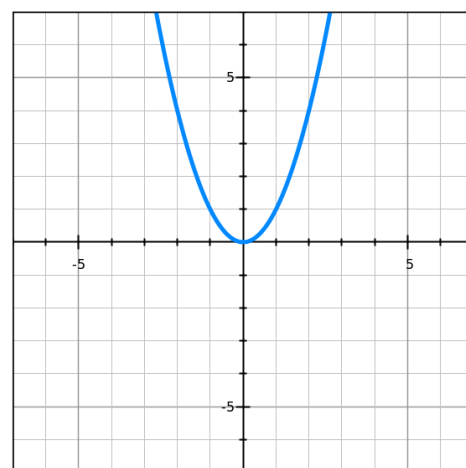
x	$g(x) = x^2 + 3$
-2	
-1	
0	
1	
2	



Contrast to Parent Function:

B. $g(x) = x^2 - 3$

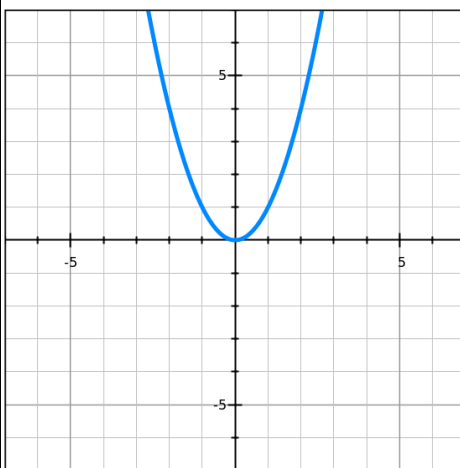
x	$g(x) = x^2 - 3$
-2	
-1	
0	
1	
2	



Contrast to Parent Function:

C. $g(x) = (x + 3)^2$

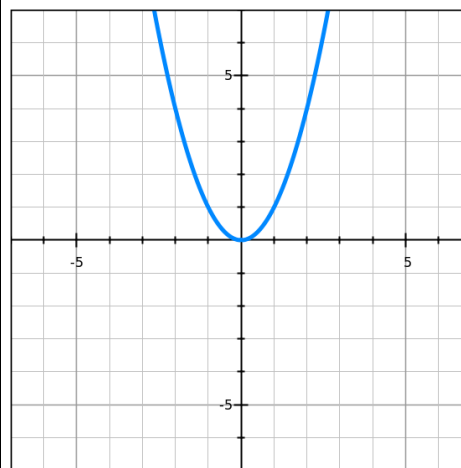
x	$g(x) = (x + 3)^2$
-5	
-4	
-3	
-2	
-1	



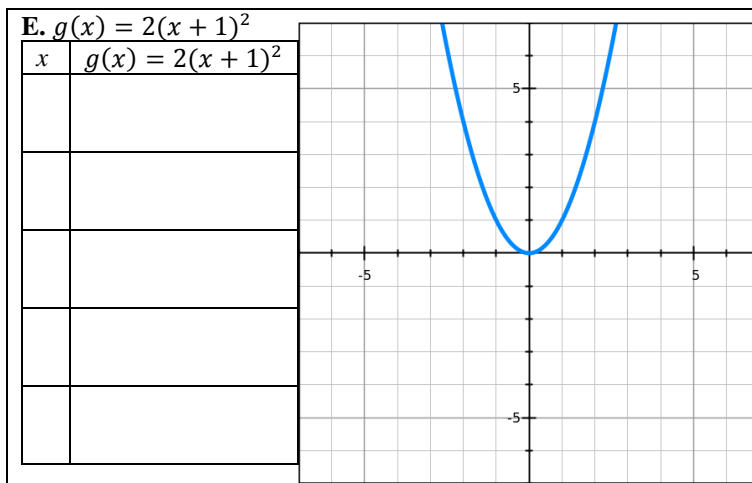
Contrast to Parent Function:

D. $g(x) = (x - 3)^2$

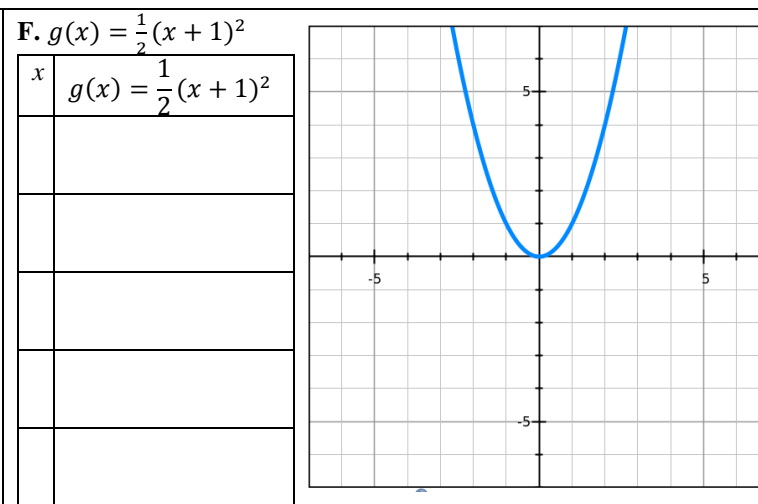
x	$g(x) = (x - 3)^2$
1	
2	
3	
4	
5	



Contrast to Parent Function:



Contrast to Parent Function:



Contrast to Parent Function:

GRAPHING QUADRATIC FUNCTIONS IN VERTEX FORM

Quadratic Functions, as well as linear, exponential, and polynomial functions, can all undergo the same types of transformations.

Type of Transformation	Example <i>Parent function: $f(x) = x^2$</i>	General Condition <i>Parent function: $f(x)$</i>
Vertical translation <i>(up or down)</i>	$g(x) = x^2 + 3$ (3 units up) $h(x) = x^2 - 1$ (1 unit down)	$f(x) + k$ $k > 0$ up $k < 0$ down
Horizontal translation <i>(to the left or right)</i>	$g(x) = (x - 4)^2$ (4 units right) $t(x) = (x + 3)^2$ (3 units left)	$f(x - h)$ $h > 0$ right $h < 0$ left [h is positive if it's right after the minus sign.]
Vertical stretch or compression	$g(x) = 3x^2$ (stretch) $h(x) = \frac{1}{3}x^2$ (compression)	$a f(x)$ $a > 1$ stretch compression $0 < a < 1$
Reflection	$g(x) = -x^2$	$-f(x)$ over x-axis opposite of

Graph $g(x) = -\frac{1}{3}(x - 6)^2 + 2$

